

Rates

Water is pumped into an underground tank at a constant rate of 8 gallons/minute. Water leaks out of the tank at the rate of $\sqrt{t+1}$ gallons per minute, for $0 \leq t \leq 120$ minutes. At time $t = 0$, the tank contains 30 gallon of water.

(a) How many gallons of water leak out of the tank from time $t = 0$ to $t = 3$ minutes?

$$\int_0^3 (8 - \sqrt{t+1}) dt$$

$$f(t) = 8t - \frac{2(t+1)^{3/2}}{3} + c$$

$c = \frac{92}{3}$

$\int_0^3 \sqrt{t+1} dt = \left(\frac{2}{3} \right)$

$t=0 \rightarrow f(t)=30$

(b) How many gallons of water are in the tank at time $t = 3$ minutes.

$$8(3) - \frac{2(3+1)^{3/2}}{3} + \frac{92}{3} = \left(\frac{148}{3} \right)$$

(c) Write an expression for $A(t)$, the total number of gallons of water in the tank at time t .

$$A(t) = 8t - \frac{2(t+1)^{3/2}}{3} + \frac{92}{3}$$

(d) At what time t , for $0 \leq t \leq 120$, is the amount of water in the tank a maximum? Justify.

$x=63$

$8 - \sqrt{t+1}$
 goes from positive to negative, which indicates a max.

t	$A'(t)$
63.99	+
63	0
63.01	-

↓
negative (a.k.a max)

Rates

The number of gallons, $P(t)$, of a pollutant in a lake changes at the rate $P'(t) = 1 - 3e^{-0.2\sqrt{t}}$ gallons per day, where t is measured in days. There are 50 gallons of the pollutant in the lake at time $t = 0$. The lake is considered to be safe when it contains 40 gallons or less of pollutant.

(a) Is the amount of pollutant increasing at time $t = 9$? Why or why not?

NO, it's decreasing. This is because the given function $P'(t) = 1 - 3e^{-0.2\sqrt{t}}$ at $t=9$ results to -0.69 , which indicates a negative rate of change, or a decrease in pollutant.

(b) For what value of t will the number of gallons of pollutant be at its minimum? Justify.

$P'(t) = 0$ $t = 30.17$

t	$P'(t)$
30.15	-
30.17	≈ 0
30.19	+

↓
Positive
(at a minimum)

(c) Is the lake safe when the number of gallons of pollutant is at its minimum? Justify.

$$50 + \int_0^{30.17} (1 - 3e^{-0.2\sqrt{t}}) dt = 35.107$$

Yes. The lake would be safe.

(d) An investigator uses the tangent line approximation to $P(t)$ at $t = 0$ as a model for the amount of pollutant in the lake. At what time t does this model predict that the lake becomes safe?

$$P'(0) = 1 - 3e^0 = -2$$

yes $50 - 2x = 40$ ~~$50 - 2x = 40$~~ ~~$50 - 2x = 40$~~ ~~$50 - 2x = 40$~~

40 = 50 - 2x

$x = 5$

$t = 5$