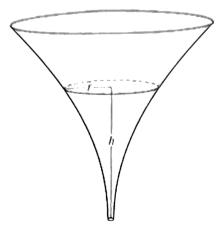
AP Calculus AB



The inside of a funnel of height 10 inches has circular cross sections, as shown in the figure above. At height h, the radius of the funnel is given by $r = \frac{1}{20}(3 + h^2)$, where $0 \le h \le 10$. The units of r and h are inches.

- (a) Find the average value of the radius of the funnel.
- (b) Find the volume of the funnel.
- (c) The funnel contains liquid that is draining from the bottom. At the instant when the height of the liquid is h = 3 inches, the radius of the surface of the liquid is decreasing at a rate of $\frac{1}{5}$ inch per second. At this instant, what is the rate of change of the height of the liquid with respect to time?

a.
$$\frac{1}{10} \int_{0}^{10} \left(\frac{1}{20} \left(3 + h^{2} \right) \right) dh = \frac{105}{60} \approx 1.816$$

$$V = \frac{1}{2\nu} \left(\frac{34\nu^2}{34\nu^2} \right)$$

$$\frac{dv}{dv} = \frac{1}{2\nu} \left(\frac{2h}{dv} \cdot \frac{dh}{dv} \right)$$

$$\frac{1}{2\nu} \left(\frac{34\nu^2}{2\nu^2} \right)$$