

Math: AP Calc AB 3.5

1. Vertical Asymptotes: N/A

Horizontal Asymptotes:

$$\lim_{x \rightarrow \infty} \frac{x+1}{\sqrt{x^2+1}} \quad \lim_{x \rightarrow -\infty} \frac{x+1}{\sqrt{x^2+1}}$$

$$= \lim_{x \rightarrow \infty} \frac{1+1/x}{\sqrt{1+1/x^2}} \quad = \lim_{x \rightarrow -\infty} \frac{1+1/x}{-\sqrt{1+1/x^2}}$$

= 1

= -1

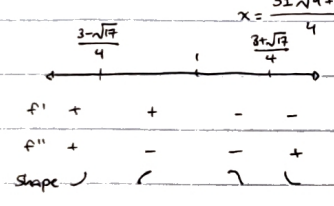
Domain: \mathbb{R} x -int: -1 y -int: 1

No symmetry

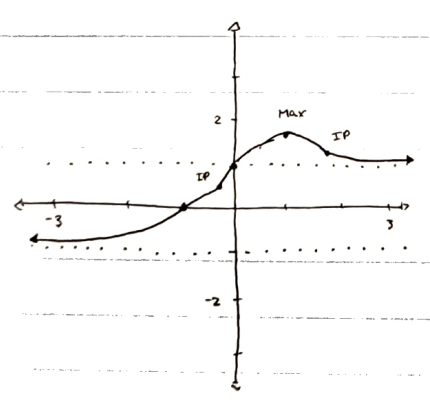
$$0 = \frac{1-x}{(x^2+1)^{3/2}} ; x=1$$

$$0 = \frac{2x^2-3x-1}{(x^2+1)^{5/2}} ; 2x^2-3x-1=0$$

$$x = \frac{3 \pm \sqrt{9+8}}{4} = \frac{3 \pm \sqrt{17}}{4} \approx -0.28, 1.78$$



Max: $(1, \sqrt{2})$ No mins
 Inflection: $(-0.28, 0.69), (1.78, 1.36)$



2. Vertical Asymptotes: $x=0$

Horizontal Asymptote:

$$\lim_{x \rightarrow \infty} \frac{\ln x}{x} = 0$$

Domain: $x \in (0, \infty)$ x -int: ~~N/A~~ 1 y -int: N/A

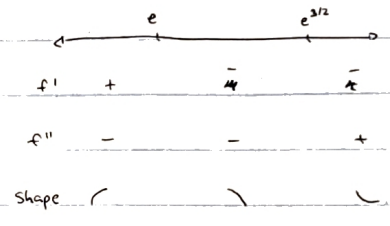
No symmetry

$$0 = \frac{1-\ln x}{x^2} ; x=e$$

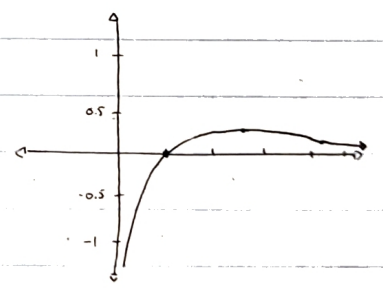
$$0 = \frac{2\ln x - 3}{x^3} ; 2\ln x - 3 = 0$$

$$\ln x = \frac{3}{2}$$

$$x = e^{3/2}$$



Max: $(e, \frac{1}{e}) \approx (2.71, 0.36)$
 Inflection: $(e^{3/2}, \frac{3}{2e^{3/2}}) \approx (4.48, 0.33)$



3. Vertical Asymptotes: $x^2+x-2=0$
 $(x+2)(x-1)=0$
 $x=-2, 1$

Horizontal Asymptotes

$$\lim_{x \rightarrow \infty} \frac{1}{x^2+x-2} = 0$$

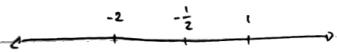
$$\lim_{x \rightarrow -\infty} \frac{1}{x^2+x-2} = 0$$

Domain: $(-\infty, -2) \cup (-2, 1) \cup (1, \infty)$ x-int: None y-int: $-\frac{1}{2}$

$$0 = \frac{-2x-1}{(x^2+x-2)^2}, \quad -2x-1=0 \quad \text{DNE at } -2, 1$$

$$x = -\frac{1}{2}$$

$$0 = \frac{6(x^2+x+1)}{(x-1)^3(x+2)^3} \quad \text{DNE at } -2, 1$$



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Max: $(-\frac{1}{2}, -\frac{4}{9})$

f'' + - - +

Shape) () (

