

DATE \_\_\_\_\_

NAME \_\_\_\_\_  
AP Calculus AB

## Practice for The Fundamental Theorem of Calculus Exam

Find the general indefinite integral for the following.

1.  $\int (\cos x - 2\sin x) dx$

~~$\cos x + \sin x + C$~~   $\boxed{2\cos x + \sin x + C}$

2.  $\int x(1+2x^4) dx$

$= \int (x + 2x^5) dx = \boxed{\frac{x^2}{2} + \cancel{2x^6} \frac{x^6}{3} + C}$

3.  $\int (x^2 + 1 + \frac{1}{x^2+1}) dx$

~~$\frac{x^3}{3} + x + \tan^{-1} x + C$~~   $\boxed{\frac{x^3}{3} + x + \tan^{-1} x + C}$

Use Part 1 of the Fundamental Theorem of Calculus to find the derivative for the following.

4.  $h(x) = \int_1^x t^2 \sin t dt$   $\boxed{x^2}$

5.  $F(x) = \int_x^5 \tan \theta d\theta = - \int_5^x \tan \theta d\theta = \boxed{1 - \tan x}$

6.  $y = \int_{e^{2x}}^0 \sin^3 t dt$

$= - \int_0^{e^{2x}} \sin^3 t dt = \sin \cancel{t} \left[ -\sin^3 e^{2x} \cdot 2e^{2x} \right]$

Use Part 2 of the Fundamental Theorem of Calculus to evaluate the integral.

7.  $\int_0^1 x^2 dx$   $F(x) = \frac{x^3}{3}$   $F(1) - F(0) = \boxed{\frac{1}{3}}$

8.  $\int_{-4}^2 \frac{2}{x^6} dx$   $F(x) = \cancel{\frac{2}{5}x^{5/5}} \quad F(2) - F(-4) = \boxed{\infty}$  ~~will do~~

9.  $\int_{-e^2}^{-e} \frac{3}{x} dx$   $3\ln|x|$   $F(-e) - F(-e^2) = \boxed{-3}$

10.  $\int_{-1}^3 |2x - x^2| dx$



$2x - x^2 = 0$

$-x^2 + 2x = 0$

$-x(x-2) = 0$

0, 2

$$\begin{aligned}
 F(x) &= \cancel{4x^3} - x^2 + \frac{x^3}{3} & F(x) &= x^2 - \frac{x^3}{3} \\
 \int_{-1}^0 (-2x + x^2) dx + \int_0^2 (2x - x^2) dx + \int_2^3 (-2x + x^2) dx \\
 &= \frac{4}{3} + \frac{4}{3} + \frac{4}{3} \\
 &= \boxed{4}
 \end{aligned}$$