## Chapter 3

Saturday, October 3, 2020 9:35 AM

- I. 3-1: Vector and Scalars
  - a. Vector: A object that has both magnitude and direction
  - b. Scalar (Quantities): Quantities that are specified by numbers or units (mass, temperature, time, etc.)
- II. 3-2: Addition of Vectors (Graphing)
  - a. One Dimensional
    - i. Finding resultant displacement: Simple Arithmetic
  - b. Two Dimensional
    - i. Finding resultant displacement:  $D_{!} = D_{"} + D_{\#} + D_{\$}$  (Note that it's not magnitude but the vector itself)
    - ii. Methods for showing resultant displacement
      - 1) Tail-to-tip Method: Adding the vectors to the previous vector
      - 2) Parallelogram Method: Adding the vectors to the starting point
- III. 3-3: Subtraction of Vectors, and Multiplication of a Vector by a Scalar
  - a. Negative Vectors: Vectors that go in the opposite direction
- IV. 3-4: Adding Vectors by Components
  - a. Vector Components:  $V_{\%}$  represents the x-axis (scalar),  $V_{\&}$  represents the y-axis (scalar)
  - b. Finding  $V_{\%}$   $V_{\&}$ ,  $\theta$  or  $V_{!}$  using SOH CAH TOA/Pythagorean Threoam
    - i.  $V_{\%} = \cos(\theta) \times V_!$

ii. 
$$V_{\&} = \sin(\theta) \times V_{!}$$

iii. 
$$V_! = 0V_{\%}^{\ \#} + V_{\&}^{\ \#}$$

iv. 
$$\theta = \tan^{(")} \left( \frac{V_{\&}}{V_{\%}} \right)$$

- V. 3-5: Projectile Motion
  - a. Finding the Peak Height
    - i. Step 1: Finding what time the peak occurred at (using vertical component)
      - 1) Use  $v_{\&} = v_{\downarrow} + gt$ , solve for t
      - 2) Final Equation:  $t = \frac{\binom{*}{1}}{+}$  ( $v_{\&}$  must be 0)
    - ii. Step 2: Using time to find the peak height (using vertical component)
      - 1) Use  $x = x_1 + v_1 t + \frac{1}{4}gt^{\#}$ , solve for x, substitute time from Step 1

2) Final Equation: 
$$x = x_1 + v_1 t + \frac{\pi}{4}gt^{\dagger}$$

- b. Finding total hang time
  - i. Step 1: Solve for time (using vertical component)

1) Use 
$$x = x_{1} + v_{1}t + \frac{\pi}{4}gt^{\#}$$
, solve for time

2) Final Equation:  $0 = \frac{\pi}{4}gt^{\#} + v_{j}t + x_{j}$  (x must equal 0, this would require quadratic formula)

$$a = \frac{\pi}{4}g$$
 (with no air resistance)

$$b = v_{j}$$

 $c = x_{j}$  (most of the time will be 0)

- c. Finding total distance traveled
  - i. Step 1: Solve for total time (using vertical component)

1) See V.b.i

- ii. Step 2: Solve for distance traveled (using horizontal component)
  - 1) Use  $x = x_1 + v_1 t + \frac{1}{4} at^{\#}$ , solve for x, substitute time from Step 1
  - 2) Final Equation:  $x = x_1 + v_1 t$  (Acceleration is 0, which cancels  $at^{\#}$ )
- d. Calculating the vector after a certain amount of time
  - i. Step 1: Finding the vertical component change (using vertical component)
    - 1) Use  $v_{\&} = v_{)} + gt$ , solve for  $v_{\&}$
  - ii. Step 2: Finding the magnitude of  $V_!$ 
    - 1) Use  $V_! = 0v_{\&}^{\#} + v_{\%}^{\#}$  solve for  $V_!$ , substitute  $v_{\&}$  with  $v_{\&}$  from Step 1
  - iii. Step 3: Finding the angle

1) 
$$\theta = \tan (" (\frac{V_{\&}}{V_{\%}}))$$

iv. Final Answer:

The vector magnitude is (answer from step 2) and it is (answer from step 3) degrees above the horizontal

- VI. 3-6: Solving Problems Involving Projectile Motion
  - a. See V.a-d
- VII. 3-7: Projectile Motion is Parabolic
  - a. The title of this section explains this section very clearly
- VIII. 3-8: Relative Velocity
  - a. Very similar to II